

# Natural paths in MCFGs

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MCFG+, Tokyo, 2010

# The interest of MCFLs

- MCFLs are defined by many independent formalisms
- MCFLs are useful for describing linguistic, biological structures

(EQ1)  $HL \subseteq MCFL$ ?

Kracht&Michaelis, Kobele: No. (Old Georgian case; Yoruba clefts)

(EQ2)  $HL \subseteq MCFL_{wn}$ ?

Joshi: Yes.  $HL \subseteq TAL=2-MCFL_{wn}$

(EQ3) 'Semantically appropriate'  $HG \subseteq MCFG$ ?

Rambow: No. (German scrambling)

These are matters of current (useful!) controversy.

## Natural paths in MCFGs

- $ML = MCFL$  (Michaelis'01, Harkema'01, Seki & al'91)
- In proving  $\subseteq$  Michaelis'98 had already revealed a 'strong' equivalence.

0. *MGs provide a succinct notation for 'strongly equivalent' MCFGs*
1. *'Order universals' derivable from fixed categories and selection features*
2. *'Improper movements' banned by fixed order of licensee features*
3. *In MCFG these are path restrictions with linear order consequences;  
allows even more succinct grammars,  
limits expressive power,  
'near' the range of Yoshinaka & Clark's learner.*

# MGs

MG =  $\langle \Sigma, \text{Cat}, \text{Ep}, \text{Lex}, M, S \rangle$  where

$\Sigma$	=	$\{\text{John, Mary, who, criticize, praise, -s, -ed, \dots}\}$	(vocabulary)
Cat	=	$\{\text{N, V, A, P, \dots}\}$	(categories)
Sel	=	$\{=f \mid f \in \text{Cat}\}$	(selectors)
Ep	=	$\{+case, +wh, +q, +foc, +top, \dots\}$	(licensors)
Lic	=	$\{-f \mid +f \in \text{Ep}\}$	(licensees)
$F$	=	$\text{Cat} \cup \text{Sel} \cup \text{Ep} \cup \text{Lic}$	
Lex	$\subseteq$	$\Sigma^\epsilon \times F^*$ , finite	(lexicon)
M	=	merge rules...	
S	$\in$	Cat	(start)

$\Sigma, \text{Cat}, \text{Sel}, \text{Ep}, \text{Lic}, \text{Lex}$  finite, non-empty, pairwise disjoint.

# 'naive Zapotec' VSO: *praised the students the idea*

the	=N	D	-ep
students	N		
idea	N		
praised	=D	V	-v
$\epsilon$	=V	+ep	=D v
$\epsilon$	=v	+ep	T
$\epsilon$	=T	+v	C

Each MG names a 'strongly equivalent'  $k$ -MCFG,  $k = |\text{Ep}| + 1$ .

# MGs as MCFGs

Given  $MG = \langle \Sigma, \text{Cat}, \text{Ep}, \text{Lex}, M, S \rangle$ , we define an MCFG with two start categories  $MG = \langle \Sigma, N, P, \{ \langle 0, S \rangle, \langle 1, S \rangle \} \rangle$ , defining the language

$$N = \{ \langle x, \delta_0, \delta_1, \dots, \delta_j \rangle \mid \begin{array}{l} x \in \{0, 1\}, \\ 0 \leq j \leq |\text{Ep}|, \\ \text{all } \delta_i \in \text{suffix}(\pi_2(\text{Lex})) \end{array} \}, \quad (1 \text{ iff } \textit{lexical})$$

where each nonterminal  $\langle x, \delta_0, \dots, \delta_j \rangle$  has rank  $j + 1$ .

# MGs as MCFGs

For  $0 \leq i, j \leq |\text{Ep}|$ ,  $\beta \neq \epsilon$ ,  $x, y \in \{0, 1\}$ :

lex: $\langle 1, \alpha \rangle(s)$	$\left. \begin{array}{l} \langle s, \alpha \rangle \in \text{Lex} \\ \\ \\ \\ \\ \\ \delta_i = -f, \text{SMC} \\ \delta_i = -f\beta, \text{SMC} \end{array} \right\}$
em1: $\langle 0, \alpha, \delta_1, \dots, \delta_j \rangle(s_0 t_0, t_1, \dots, t_j) :-$ $\langle 1, =f\alpha \rangle(s_0),$ $\langle x, f, \delta_1, \dots, \delta_j \rangle(t_0, \dots, t_j)$	
em2: $\langle 0, \alpha, \delta_1, \dots, \delta_i, \gamma_1, \dots, \gamma_j \rangle(t_0 s_0, s_1, \dots, s_i, t_1, \dots, t_j) :-$ $\langle 0, =f\alpha, \delta_1, \dots, \delta_i \rangle(s_0, \dots, s_i),$ $\langle x, f, \gamma_1, \dots, \gamma_j \rangle(t_0, \dots, t_j)$	
em3: $\langle 0, \alpha, \beta, \delta_1, \dots, \delta_i, \gamma_1, \dots, \gamma_j \rangle(s_0, t_0, s_1, \dots, s_i, t_1, \dots, t_j) :-$ $\langle x, =f\alpha, \delta_1, \dots, \delta_i \rangle(s_0, \dots, s_i),$ $\langle y, f\beta, \gamma_1, \dots, \gamma_j \rangle(t_0, \dots, t_j)$	
im1: $\langle 0, \alpha, \delta_1, \dots, \delta_{i-1}, \delta_{i+1}, \dots, \delta_j \rangle(s_i s_0, s_1, \dots, s_{i-1}, s_{i+1}, \dots, s_j) :-$ $\langle 0, +f\alpha, \delta_1, \dots, \delta_j \rangle(s_0, \dots, s_j)$	
im2: $\langle 0, \alpha, \delta_1, \dots, \delta_{i-1}, \beta, \delta_{i+1}, \dots, \delta_j \rangle(s_0, \dots, s_i) :-$ $\langle 0, +f\alpha, \delta_1, \dots, \delta_j \rangle(s_0, \dots, s_i)$	

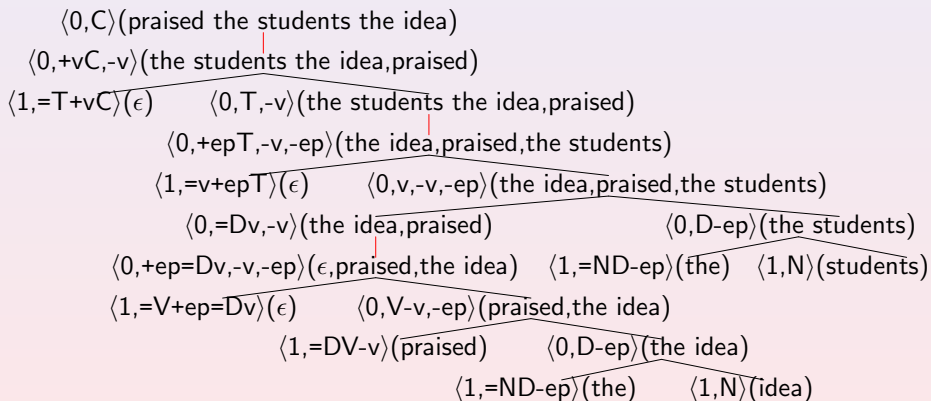
SMC:  $\delta_1, \dots, \delta_{i-1}, \delta_{i+1}, \dots, \delta_j$  do not begin with -f.

# 'naive Zapotec' VSO: *praised the students the idea*

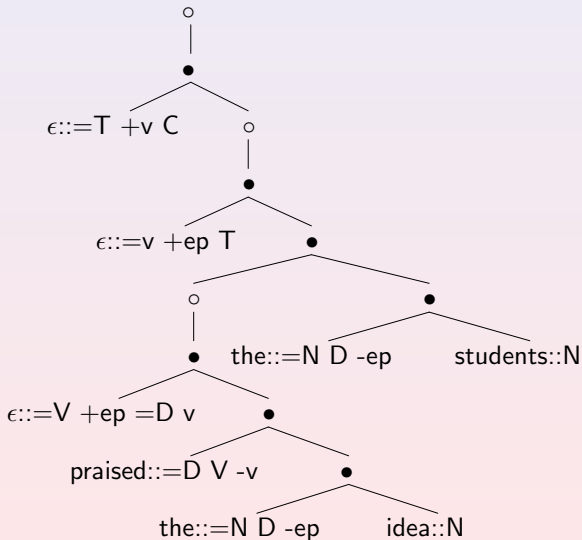
the	=N	D	-ep
students	N		
idea	N		
praised	=D	V	-v
ε	=V	+ep	=D v
ε	=v	+ep	T
ε	=T	+v	C



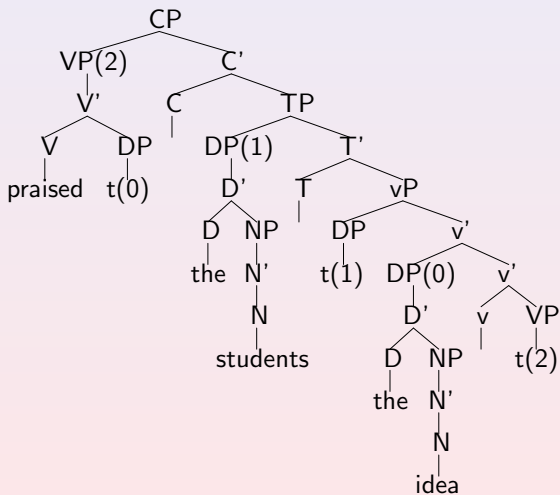
# 'naive Zapotec' VSO: *praised the students the idea*



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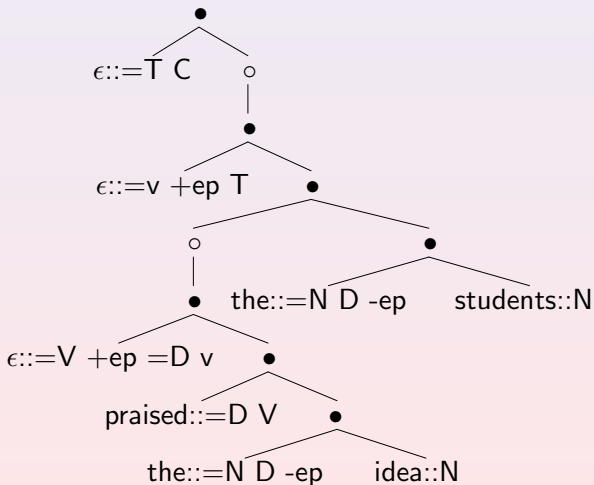


'naive Zapotec' VSO: *praised the students the idea*

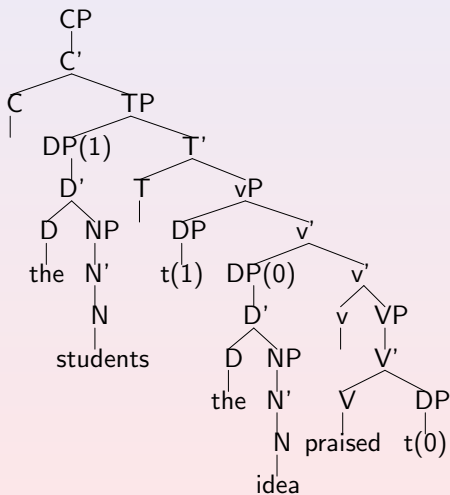


# 'naive Tamil' SOV: *the students the idea praised*

the	=N D -ep
students	N
idea	N
praised	=D V
$\epsilon$	=V +ep =D v
$\epsilon$	=v +ep T
$\epsilon$	=T C

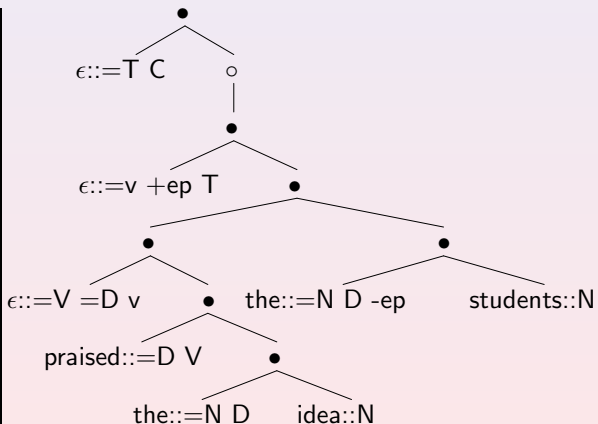


# 'naive Tamil' SOV: *the students the idea praised*

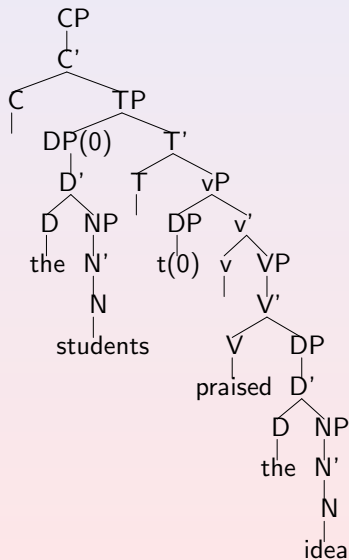


# 'naive English' SVO: *the students praised the idea*

the	=N D
the	=N D -ep
students	N
idea	N
praised	=D V
$\epsilon$	=V =D v
$\epsilon$	=v +ep T
$\epsilon$	=T C
which	=N D -wh
which	=N D -ep -wh
teachers	N
$\epsilon$	=T +wh C
knew	=D V

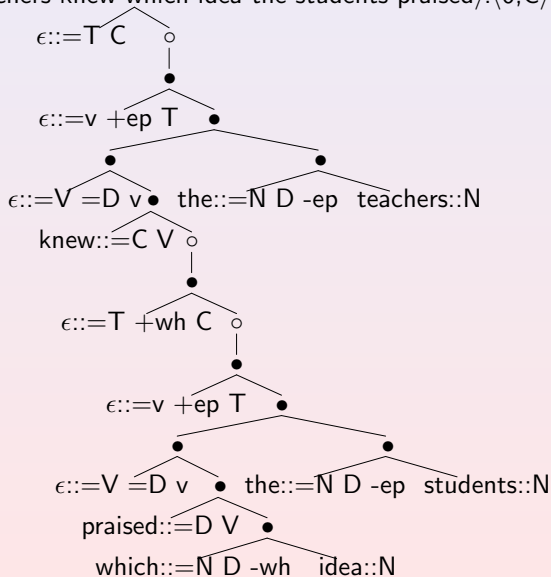


'naive English' SVO: *the students praised the idea*



# 'naive English' SVO

⟨the teachers knew which idea the students praised⟩:(0,C)





# 'naive English' SVO MCFG (page 1)

the	=N D
the	=N D -ep
students	N
idea	N
praised	=D V
ε	=V =D v
ε	=v +ep T
ε	=T C
which	=N D -wh
which	=N D -ep -wh
teachers	N
ε	=T +wh C
knew	=C V

$\langle 0, C \rangle (s_0 t_0) : - \langle 1, =T C \rangle (s_0), \langle 0, T \rangle (t_0)$   
 $\langle 1, =T C \rangle (\epsilon)$   
 $\langle 0, T \rangle (s_1 s_0) : - \langle 0, +ep T, -ep \rangle (s_0, s_1)$   
 $\langle 0, +ep T, -ep \rangle (s_0 t_0, t_1) : - \langle 1, =v +ep T \rangle (s_0), \langle 0, v, -ep \rangle (t_0, t_1)$   
 $\langle 1, =v +ep T \rangle (\epsilon)$   
 $\langle 0, v, -ep \rangle (s_0, t_0) : - \langle 0, =D v \rangle (s_0), \langle 0, D -ep \rangle (t_0)$   
 $\langle 0, =D v \rangle (s_0 t_0) : - \langle 1, =V =D v \rangle (s_0), \langle 0, V \rangle (t_0)$   
 $\langle 1, =V =D v \rangle (\epsilon)$   
 $\langle 0, V \rangle (s_0 t_0) : - \langle 1, =C V \rangle (s_0), \langle 0, C \rangle (t_0)$   
 $\langle 1, =C V \rangle (\text{knew})$   
 $\langle 0, C \rangle (s_1 s_0) : - \langle 0, +wh C, -wh \rangle (s_0, s_1)$   
 $\langle 0, +wh C, -wh \rangle (s_0 t_0, t_1) : - \langle 1, =V +wh C \rangle (s_0), \langle 0, V, -wh \rangle (t_0, t_1)$   
 $\langle 1, =V +wh C \rangle (\epsilon)$   
 $\langle 0, V, -wh \rangle (s_0 t_0, t_1) : - \langle 1, =C V \rangle (s_0), \langle 0, C, -wh \rangle (t_0, t_1)$   
 $\langle 0, C, -wh \rangle (s_0 t_0, t_1) : -em_1 [ \langle 1, =T C \rangle (s_0), \langle 0, T, -wh \rangle (t_0, t_1) ]$

.....

## 'naive English' SVO MCFG (page 2)

... ..

$\langle 0, T, -wh \rangle(s_2 s_0, s_1) :- \langle 0, +ep T, -wh, -ep \rangle(s_0, s_1, s_2)$

$\langle 0, +ep T, -wh, -ep \rangle(s_0 t_0, t_1, t_2) :- \langle 1, =v +ep T \rangle(s_0), \langle 0, v, -wh, -ep \rangle(t_0, t_1, t_2)$

$\langle 0, v, -wh, -ep \rangle(s_0, s_1, t_0) :- \langle 0, =D v, -wh \rangle(s_0, s_1), \langle 0, D -ep \rangle(t_0)$

$\langle 0, =D v, -wh \rangle(s_0 t_0, t_1) :- \langle 1, =V =D v \rangle(s_0), \langle 0, V, -wh \rangle(t_0, t_1)$

$\langle 0, V, -wh \rangle(s_0, t_0) :- \langle 1, =D V \rangle(s_0), \langle 0, D -wh \rangle(t_0)$

$\langle 1, =D V \rangle(\text{praised})$

$\langle 0, D -wh \rangle(s_0 t_0) :- \langle 1, =N D -wh \rangle(s_0), \langle 1, N \rangle(t_0)$

$\langle 1, =N D -wh \rangle(\text{which})$

$\langle 1, N \rangle(\text{teachers})$

$\langle 1, N \rangle(\text{idea})$

$\langle 1, N \rangle(\text{students})$

$\langle 0, D -ep \rangle(s_0 t_0) :- \langle 1, =N D -ep \rangle(s_0), \langle 1, N \rangle(t_0)$

$\langle 1, =N D -ep \rangle(\text{the})$

$\langle 0, T, -wh \rangle(s_1 s_0, s_2) :- \langle 0, +ep T, -ep, -wh \rangle(s_0, s_1, s_2)$

$\langle 0, +ep T, -ep, -wh \rangle(s_0 t_0, t_1, t_2) :- \langle 1, =v +ep T \rangle(s_0), \langle 0, v, -ep, -wh \rangle(t_0, t_1, t_2)$

... ..

# 'naive English' SVO MCFG (page 3)

	...	...	
$\langle 0, v, -ep, -wh \rangle(s_0, s_1, t_0)$	$:-$	$\langle 0, =D v, -ep \rangle(s_0, s_1), \langle 0, D -wh \rangle(t_0)$	
$\langle 0, =D v, -ep \rangle(s_0 t_0, t_1)$	$:-$	$\langle 1, =V =D v \rangle(s_0), \langle 0, V, -ep \rangle(t_0, t_1)$	
$\langle 0, V, -ep \rangle(s_0, t_0)$	$:-$	$\langle 1, =D V \rangle(s_0), \langle 0, D -ep \rangle(t_0)$	
$\langle 0, T, -wh \rangle(s_0, s_1)$	$:-$	$\langle 0, +ep T, -ep -wh \rangle(s_0, s_1)$	
$\langle 0, +ep T, -ep -wh \rangle(s_0 t_0, t_1)$	$:-$	$\langle 1, =v +ep T \rangle(s_0), \langle 0, v, -ep -wh \rangle(t_0, t_1)$	
$\langle 0, v, -ep -wh \rangle(s_0, t_0)$	$:-$	$\langle 0, =D v \rangle(s_0), \langle 0, D -ep -wh \rangle(t_0)$	
$\langle 0, D -ep -wh \rangle(s_0 t_0)$	$:-$	$\langle 1, =N D -ep -wh \rangle(s_0), \langle 1, N \rangle(t_0, t_1)$	
$\langle 1, =N D -ep -wh \rangle(\text{which})$			
$\langle 0, v, -ep -wh \rangle(t_0 s_0, s_1)$	$:-$	$\langle 0, =D v, -ep -wh \rangle(s_0, s_1), \langle 0, D \rangle(t_0)$	
$\langle 0, =D v, -ep -wh \rangle(s_0 t_0, t_1)$	$:-$	$\langle 1, =V =D v \rangle(s_0), \langle 0, V, -ep -wh \rangle(t_0, t_1)$	
$\langle 0, V, -ep -wh \rangle(s_0, t_0)$	$:-$	$\langle 1, =D V \rangle(s_0) \langle 0, D -ep -wh \rangle(t_0)$	
$\langle 0, D \rangle(s_0 t_0)$	$:-$	$\langle 1, =N D \rangle(s_0), \langle 1, N \rangle(t_0)$	
$\langle 1, =N D \rangle(\text{the})$			
$\langle 0, V \rangle(s_0 t_0)$	$:-$	$\langle 1, =D V \rangle(s_0), \langle 0, D \rangle(t_0)$	
$\langle 0, v, -ep \rangle(t_0 s_0, s_1)$	$:-$	$\langle 0, =D v, -ep \rangle(s_0, s_1), \langle 0, D \rangle(t_0)$	

## Constituent order

- MG builds spec-head-comp, which can then be distorted by movements.

=D =D V is analagous to  $(D \setminus V) / D$ .

MG has no analog of changing slash direction. Alternative orders by movement to the left, introducing asymmetries. . .

- Cinque'05, Greenberg'63 Universal 20:  
not all orders of [Dem Num Adj N] are attested
- Given [1 [2 [3 [4]]]], what orders by adding 'licensing'?

# Constituent order

order	C	MG	order	C	MG
1234	<b>4</b>	<b>4</b>	1324	<b>0</b>	<b>0</b>
1243	<b>3</b>	<b>3</b>	1342	<b>1</b>	<b>3</b>
1423	<b>1</b>	<b>3</b>	1432	<b>3</b>	<b>2</b>
4123	<b>2</b>	<b>3</b>	4132	<b>1</b>	<b>2</b>
2134	<b>0</b>	<b>0</b>	2314	<b>0</b>	<b>0</b>
2143	<b>0</b>	<b>0</b>	2341	<b>1</b>	<b>3</b>
2413	<b>0</b>	<b>0</b>	2431	<b>2</b>	<b>2</b>
4213	<b>0</b>	<b>0</b>	4231	<b>2</b>	<b>2</b>
3124	<b>0</b>	<b>0</b>	3214	<b>0</b>	<b>0</b>
3142	<b>0</b>	<b>2</b>	3241	<b>0</b>	<b>0</b>
3412	<b>1</b>	<b>3</b>	3421	<b>1</b>	<b>2</b>
4312	<b>2</b>	<b>2</b>	4321	<b>4</b>	<b>2</b>

	Cinque	MG
0=	unattested	underivable
1=	very few	4 licensors
2=	few	3 licensors
3=	many	2 licensors
4=	very many	0-1 licensors

# Constituent order

order	C	MG	order	C	MG
1234	4	4	1324	0	0
1243	3	3	1342	1	3
1423	1	3	1432	3	2
4123	2	3	4132	1	2
2134	0	0	2314	0	0
2143	0	0	2341	1	3
2413	0	0	2431	2	2
4213	0	0	4231	2	2
3124	0	0	3214	0	0
3142	0	2	3241	0	0
3412	1	3	3421	1	2
4312	2	2	4321	4	2

	Cinque	MG
0=	unattested	underivable
1=	very few	4 licensors
2=	few	3 licensors
3=	many	2 licensors
4=	very many	0-1 licensors

## Constituent order

- MG hypothesis explains U20 only with fixed selection

Dem < Num < Adj < N

MG allows no change in slash direction; now, no change in selection..

(Makes sense only with independent properties. 'Flexible' accounts similar.)

- Our VSO, SOV, VSO examples:

C < T < v < V < D < N

- Rizzi'04 'left periphery'

Force < Top1 < Foc < Top2 < Fin < Infl

- Cinque'99 adverbials

Mood < Evidential < Epistemic < Habitual < Inceptive  
frankly    allegedly    probably    usually    suddenly

- Manzini&Savoia'04 clitic positions

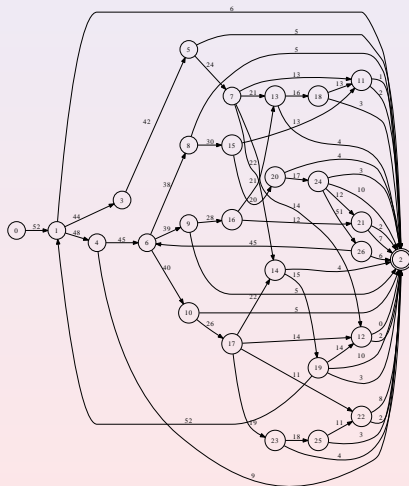
Def(uninfl) < Quant(3) < N(3pl) < P(1,2) < Origin < Loc < Measure

# Constituent order and paths

- **(Cartographic hypothesis)** (informal)  
Categories and order of selection in human languages is universal.  
'Clausal hierarchy is fixed.'
- 'C-selection' looks like it might be semantically motivated.  
Could 'c-selection' be completely reduced to 's-selection'?  
Chomsky'95 speculates: "there is a syntactic residue" (p.33)
- For any CFG, path language regular (Thatcher'67)



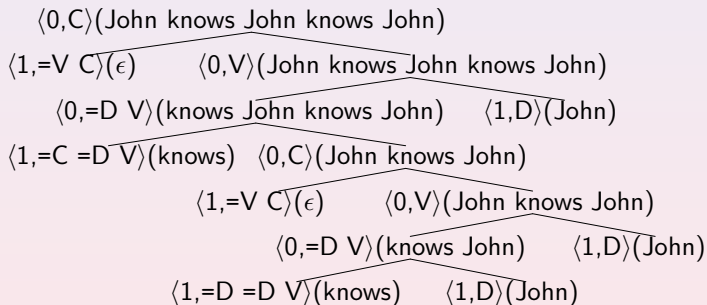
# Paths in naive English



Naive English is slightly complicated, so consider this 'tiny English'...

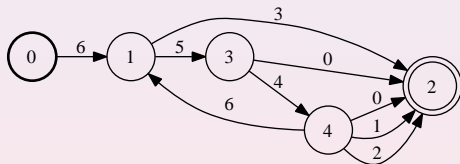
# Tiny English

John	D
knows	=D =D V
knows	=C =D V
$\epsilon$	=V C



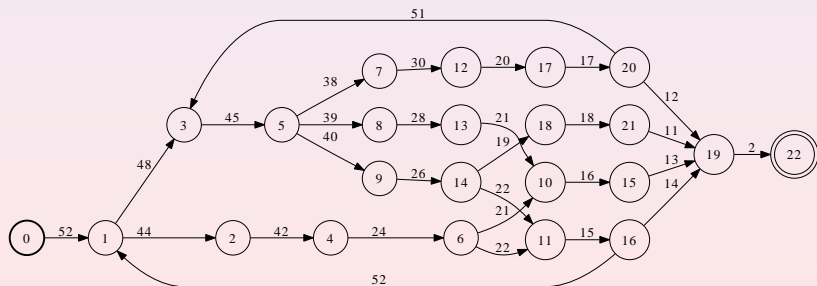
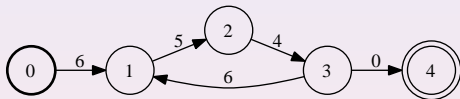
# Tiny English

$0 = \langle 1, D \rangle$        $1 = \langle 1, =D=DV \rangle$        $2 = \langle 1, =C=DV \rangle$        $3 = \langle 1, =VC \rangle$   
 $4 = \langle 0, =DV \rangle$        $5 = \langle 0, V \rangle$                        $6 = \langle 0, C \rangle$



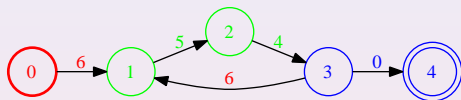
- Path sets strictly 2-local (2-SL), as for any CFG
- Last symbol a terminal category, which never dominates anything.
- ‘spine’: at binary branches, the right sister; otherwise left sister.

# Spinal paths

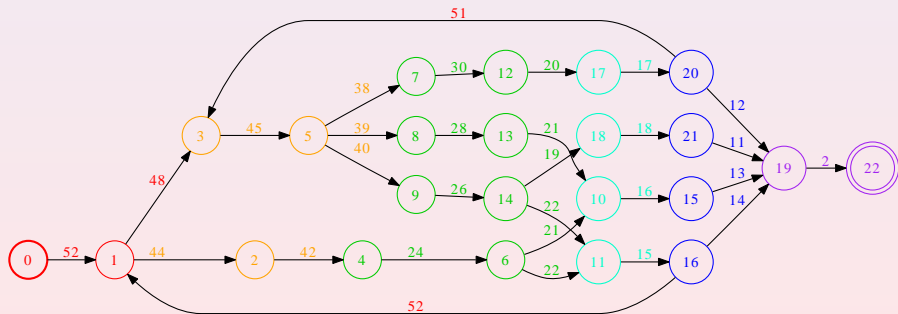


# Spinal paths

tiny English: C, V, D:



Naive English: C, T, v, V, D, N:



# 'Cartography'

- **(Cartographic hypothesis CH1)** UG fixes  $\text{Cat}_{\leq}$  so that
  - If  $fg$  appears in a spinal path and  $f \neq g$ , then either  $f$  covers $_{\leq} g$  or  $g$  minimal $_{\leq}$ .*
  - If  $fg$  appears in a non-spinal path initiated at a spec position, and  $f \neq g$ , then either  $f$  covers $_{\leq} g$  or  $g$  minimal $_{\leq}$ .*

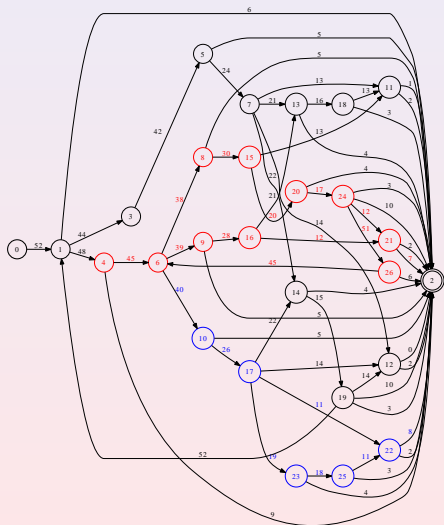
# Movement order universals

- Naive English *which idea* moves twice, with  $-ep$   $-wh$   
the teachers knew which idea<sub>*i*</sub>; the students *t<sub>i</sub>* praised *t<sub>i</sub>*

(BOIM) Other orders are 'improper', yielding ungrammaticality

- \* Who<sub>*i*</sub> seems *t<sub>i</sub>* will *t<sub>i</sub>* leave?
- \* Who<sub>*i*</sub> seems it is likely *t<sub>i</sub>* to *t<sub>i</sub>* leave?
- $ep \triangleleft \text{scrambling} \triangleleft wh \triangleleft \text{top}$  (Abels'07)

# Movement order universals: naive English -wh and -ep-wh



MGs would allow -ep to -wh-ep equally easily, but that never happens!



## Path restrictions 2

**(Cartographic hypothesis CH2)** Movement features  $E_{p_{\triangleleft}}$  are ordered so that if a component moves for  $g$  and then for  $f$ ,  $f \triangleleft g$

MG allows Lex to generate paths violating these conditions, but we can block that...

## Ordered MGs

$$\text{OMG} = \langle \Sigma, \text{Cat}_{\leq}, \text{Ep}_{\triangleleft}, \text{Df}, \mu, \text{Lex}, \text{M}, \text{S} \rangle$$

$\Sigma$	=	{John, Mary, who, criticize, praise, -s, -ed, ...}	(vocabulary)
Cat	=	$\langle \{N, V, A, P, \dots\}, \leq \rangle$	(categories)
Ep	=	$\langle \{\text{case, wh, q, foc, top, \dots}\}, \triangleleft \rangle$	(licensors)
Df	:	$\text{Cat} \rightarrow \text{Cat} \cup \text{Ep}$	(deficiencies)
$\mu$	=	meanings, e.g. $\text{TH}(E, 2, S)$	(extends to $\llbracket \cdot \rrbracket$ )
Lex	$\subseteq$	$\Sigma^e \times \text{Cat} \times \wp(\text{Ep}) \times \mu$	(lexicon)
M	=	merge, the union of EM and IM rules	
S	$\in$	Cat	(start)

- $a$  selects  $b$  iff  $a$  covers $_{\leq}$   $b$  or  $b$  minimal $_{\triangleleft}$
- Semantic type may restrict selection and deficiency
- Df maps each Cat to at most one value – at most one specifier..

Many linguists assume  $\text{UG} = \langle \text{Cat}_{\leq}, \text{Ep}_{\triangleleft}, \text{Df}, \text{M}, \text{S} \rangle$ ; all variation in Lex.

# Ordered MGs

the	=N D
the	=N D -ep
students	N
idea	N
praised	=D V
ε	=V =D v
ε	=v +ep T
ε	=T C
which	=N D -wh
which	=N D -ep -wh
teachers	N
ε	=T +wh C
knew	=C V

C<T<v<V<D<N	
wh<ep	
Df: C→wh, T→ep, v→ep	
the	D
the	D {ep}
students	N
idea	N
praised	V
ε	v
ε	T
ε	C
which	D {wh}
which	D {ep,wh}
teachers	N
ε	C
knew	V

# Ordered MGs

## Expressive power

- $\forall UG, OML_{UG} \subsetneq (|E_p| + 1)\text{-MCFL}(2) \subsetneq \text{MCFL}$   
(Seki et al'91; Rambow&Satta'99)

## Learnability

- $\forall UG, OML_{UG}$  finite, hence identifiable from positive text
- $p$ -congruential MCFLs are identifiable from membership queries (yes or no to  $x \in L_*$ ?) and equivalence queries (yes or counterexample to  $L = L_*$ ?).  
(Yoshinaka&Clark'10)

$G \in p\text{-MCFG}(r)$  is  $p$ -congruential iff

(i) string functions linear and non-permuting, and

(ii) for every nonterminal  $A$ , and any  $\mathbf{u}, \mathbf{v} \in L(G, A)$ ,  $L(G)/\mathbf{u} = L(G)/\mathbf{v}$ .

# Non-permuting OMGs

MGs, OMGs have this permuting rule, when  $\delta_i = -f$ , SMC:

$$\text{im1: } \langle 0, \alpha, \delta_1, \dots, \delta_{i-1}, \delta_{i+1}, \dots, \delta_j \rangle (s_i s_0, s_1, \dots, s_{i-1}, s_{i+1}, \dots, s_j) :- \\ \langle 0, +f\alpha, \delta_0, \dots, \delta_j \rangle (s_0, \dots, s_j)$$

? Can we change this to something like:

$$\text{im1???: } \langle 0, \delta_1, \dots, \delta_{i-1}, \alpha \rangle (s_1, \dots, s_{i-1}, s_i s_0) :- \\ \langle 0, \delta_1, \dots, \delta_i, +f\alpha \rangle (s_1, \dots, s_i, s_0)$$

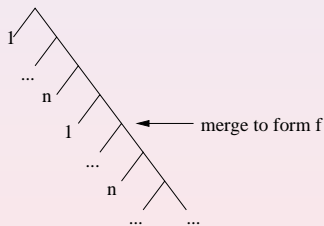
Yes, for certain OMGs we can formulate (strongly equivalent) non-permuting rules. E.g. suppose  $\leq, \triangleleft$  total, Df total and 1-1...

## Non-permuting OMGs

To form a constituent of category  $f$  with the components

$$\alpha f \beta, \delta_1, \dots, \delta_i, \gamma_1, \dots, \gamma_j.$$

Is it possible to determine the surface order of these elements? Yes.  
Suppose  $Cat = \{1, \dots, n\}$  where  $\forall c \in cat, c \mapsto +c$  and  $\beta = -i-j-k$ :



If  $f \leq i$ , then  $-i$  checked at  $i$ ,  $(i - f)$  steps away.

Then if  $j \leq i$ ,  $-j$  checked at  $j$ ,  $(j - i) + (i - f)$  steps away.

Then if  $k \leq j$ ,  $-k$  checked at  $j$ ,  $(k - j) + (j - i) + (i - f)$  steps away.

Other cases similarly.

## OMGs as MCFGs

$$\text{em1: } \langle 0, \delta_0, \dots, \delta_{i-1}, \alpha, \delta_{i+1}, \dots, \delta_j \rangle (t_0, \dots, t_{i-1}, s_0 t_i, t_{i+1}, \dots, t_j) :- \\ \langle 1, =f\alpha \rangle (s_0), \\ \langle x, \delta_0, \dots, \delta_{i-1}, f, \delta_{i+1}, \dots, \delta_j \rangle (t_0, \dots, t_j)$$

$$\text{em2: } \langle 0, \eta_0, \dots, \eta_{j+l+1} \rangle (u_0, \dots, u_{j+l+1}) :- \\ \langle 0, \delta_0, \dots, \delta_{i-1}, =f\alpha, \delta_{i+1}, \dots, \delta_j \rangle (s_0, \dots, s_j), \\ \langle x, \gamma_0, \dots, \gamma_{j-1}, f, \gamma_{j+1}, \dots, \gamma_\ell \rangle (t_0, \dots, t_\ell)$$

where  $\eta_0, \dots, \eta_{j+l+1}$  is the sort of

$\delta_0, \dots, \delta_{i-1}, \alpha, \delta_{i+1}, \dots, \delta_j, \gamma_0, \dots, \gamma_{k-1}, \gamma_{k+1}, \dots, \gamma_\ell$ , and

$u_0, \dots, u_{j+l+1}$  the corresponding sort of

$s_0, \dots, s_{i-1}, t_k s_i, s_{i+1}, \dots, s_j, t_0, \dots, t_{k-1}, t_{k+1}, \dots, t_\ell$ .

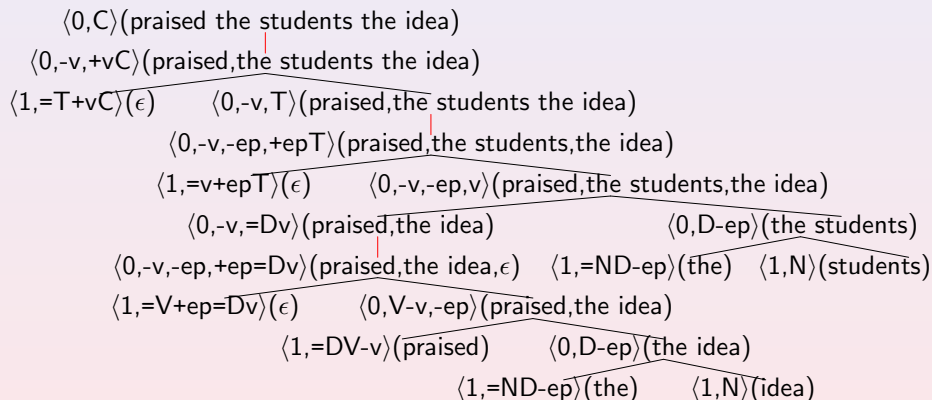
$$\text{em3: } \langle 0, \eta_0, \dots, \eta_{j+l+2} \rangle (u_0, \dots, u_{j+l+2}) :- \\ \langle x, \delta_0, \dots, \delta_{i-1}, =f\alpha, \delta_{i+1}, \dots, \delta_j \rangle (s_0, \dots, s_j), \\ \langle y, \gamma_0, \dots, \gamma_{j-1}, f\beta, \gamma_{j+1}, \dots, \gamma_\ell \rangle (t_0, \dots, t_\ell)$$

where  $\eta_0, \dots, \eta_{j+l+2}$  is the sort of

$\delta_0, \dots, \delta_{i-1}, \alpha, \delta_{i+1}, \dots, \delta_j, \gamma_0, \dots, \gamma_{k-1}, \beta, \gamma_{k+1}, \dots, \gamma_\ell$ , and

$u_0, \dots, u_{j+l+2}$  the corresponding sort of  $s_0, \dots, s_j, t_0, \dots, t_\ell$ .

## non-permuting 'naive Zapotec'



- Non-permuting, and well-nested!
- Unlike many  $E_{p+1}$ -MCFG hypotheses, 'semantically coherent'



## SpIC-violating non-permuting well-nested OMG

- non-permuting, well-nested movements may violating SpIC – when Spec components do not move higher than components of selecting clause

$$\text{em2: } \langle 0, \eta_0, \dots, \eta_{j+l+1} \rangle (u_0, \dots, u_{j+l+1}) :- \\ \langle 0, \delta_0, \dots, \delta_{i-1}, =f\alpha, \delta_{i+1}, \dots, \delta_j \rangle (s_0, \dots, s_j), \\ \langle x, \gamma_0, \dots, \gamma_{j-1}, f, \gamma_{j+1}, \dots, \gamma_\ell \rangle (t_0, \dots, t_\ell)$$

where  $\eta_0, \dots, \eta_{j+l+1}$  is the sort of

$\delta_0, \dots, \delta_{i-1}, \alpha, \delta_{i+1}, \dots, \delta_j, \gamma_0, \dots, \gamma_{k-1}, \gamma_{k+1}, \dots, \gamma_\ell$ .

Cf. informal discussions of conditions on “surfing” movement (Sauerland'96, Abels'07, ...)

# Conclusions

- MGs provide a succinct notation for ‘strongly equivalent’ MCFGs
- OMGs provide posets  $\text{Cat}_{\leq}$ ,  $\text{Ep}_{\triangleleft}$ 
  - Selection can be restricted with  $\leq$  for ‘Order universals’
  - Movement can be restricted with  $\triangleleft$  for ‘BOIM’
  - More succinct than strongly equivalent MGs, MCFGs.
  - Finite class  $\text{OML}_{\text{UG}} \subsetneq (|\text{Ep}| + 1)\text{-MCFL}(2) \subsetneq \text{MCFL}$
  - Some OMGs have non-permuting strong equivalents, intersecting with the range of Yoshinaka&Clark’s learner.  
And some of these are well-nested.

(Q) For which UG,  $\subseteq \text{OMG}_{\text{ug}}$  non-permuting?

(Q) For which UG,  $\subseteq \text{OMG}_{\text{ug}}$  well-nested?

(EQ4) ‘Semantically appropriate’  $\text{HG} \subseteq \text{MCFG}_{\text{wn}}$ ?



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